

# Probability problem solving 2

Next

Date: \_\_\_\_\_

## Probability problem solving 2

Sit down with a pen and paper.



Calculator allowed

You need to complete probability problem solving 1 before doing this lesson.



All 7 events were carried out for real.

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 1        |              |           |
| 2        |              |           |
| 3        |              |           |
| 4        |              |           |
| 5        |              |           |
| 6        |              |           |
| 7        |              |           |

The aim is to get as many counters as possible by making smart choices.

# Bet 4

Back

1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters



Take the bet

What's my chances?

Not playing

# What are my chances?

Back Next

1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters



To understand this problem we need to consider all the possible outcomes.

We can do this by drawing a **sample space diagram**.

# What are my chances?

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1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters



Dice 2

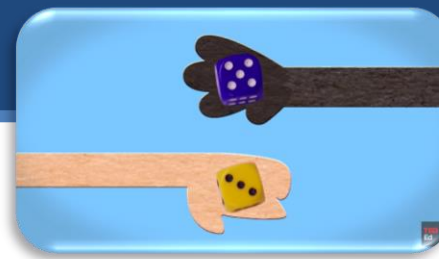
|   | 1   | 2   | 3   | 4   | 5   | 6   |
|---|-----|-----|-----|-----|-----|-----|
| 1 | 1,1 | 1,2 | 1,3 | 1,4 | 1,5 | 1,6 |
| 2 | 2,1 | 2,2 | 2,3 | 2,4 | 2,5 | 2,6 |
| 3 | 3,1 | 3,2 | 3,3 | 3,4 | 3,5 | 3,6 |
| 4 | 4,1 | 4,2 | 4,3 | 4,4 | 4,5 | 4,6 |
| 5 | 5,1 | 5,2 | 5,3 | 5,4 | 5,5 | 5,6 |
| 6 | 6,1 | 6,2 | 6,3 | 6,4 | 6,5 | 6,6 |

Dice 1

Outcomes

# What are my chances?

Back Next



1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters

Dice 2

|   | 1   | 2   | 3   | 4   | 5   | 6   |
|---|-----|-----|-----|-----|-----|-----|
| 1 | 1,1 | 1,2 | 1,3 | 1,4 | 1,5 | 1,6 |
| 2 | 2,1 | 2,2 | 2,3 | 2,4 | 2,5 | 2,6 |
| 3 | 3,1 | 3,2 | 3,3 | 3,4 | 3,5 | 3,6 |
| 4 | 4,1 | 4,2 | 4,3 | 4,4 | 4,5 | 4,6 |
| 5 | 5,1 | 5,2 | 5,3 | 5,4 | 5,5 | 5,6 |
| 6 | 6,1 | 6,2 | 6,3 | 6,4 | 6,5 | 6,6 |

Dice 1

You win

You lose

# What are my chances?

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1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters



1 How many outcomes are there?

2 How many desired outcomes are there?

Lets say you roll the dice **36 times** and **win 16** of them.

3 How much have you paid to play?

4 How much have you won?

5 How much have you lost altogether?

6 How would the answer to **Q5** change if you rolled **360 times** instead?

This is what we expect to happen.

1 counter to play

Roll 2 dice

If both numbers are 4 or less you win 2 counters



1 How many outcomes are there? **36 outcomes**

2 How many desired outcomes are there? **16 desired outcomes**

Lets say you roll the dice **36 times** and **win 16** of them.

3 How much have you paid to play? **36 counters**

4 How much have you won? **32 counters**

5 How much have you lost altogether? **4 counters**

**40 counters**

6 How would you expect **Q5** to change if you rolled **360 times** instead?



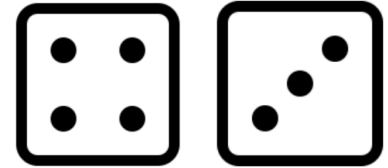
# Update your table

Back Next

1 counter to play

Roll 2 dice

Outcome



If both numbers are 4 or less you win 2 counters

Looks like you were lucky.

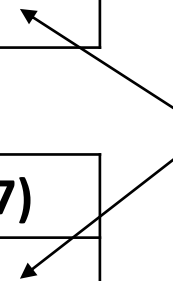
Take the bet

| Question | +/- Counters  | Total (7) |
|----------|---------------|-----------|
| 4        | $-1 + 2 = +1$ |           |

Not playing

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 4        | 0            |           |

Update



1 counter to play

Look out the window

If the next car that drives past is  
grey you win 3 counters



Take the bet

What's my chances?

Not playing

In 2018, grey became the UK's most popular car colour with **495,127** new models bearing the shade, **up 1.2% on 2017**.

# What are my chances?

Back Next

1 counter to play

Look out the window

If the next car that drives past is  
grey you win 3 counters



Although this is true –

*“In 2018, grey became the UK’s most popular car colour with **495,127** new models bearing the shade, **up 1.2% on 2017.**”*

It doesn’t say what proportion of cars are grey. It turns out  $\approx 20\%$  of cars are grey.

$$20\% = 0.2 = \frac{1}{5}$$

# What are my chances?

Back Next

1 counter to play

Look out the window

If the next car that drives past is grey you win 3 counters



1 If 100 cars drive past, how many do you expect to be grey?

2 If 20 cars drive past, how many do you expect to be grey?

Lets say you watch **10 cars** drive past and **two are grey**.

3 How much have you paid to play?

← This is what we expect to happen.

4 How many counters have you taken for your winnings?

5 How much have you lost altogether?

1 counter to play

Look out the window

If the next car that drives past is grey you win 3 counters



1 If 100 cars drive past, how many do you expect to be grey? **20**

2 If 20 cars drive past, how many do you expect to be grey?

Lets say you watch **10 cars** drive past and **two are grey**.  $\frac{1}{5} \times 20 = 4$

3 How much have you paid to play? **10 counters**

4 How many counters have you taken for your winnings? **6 counters**

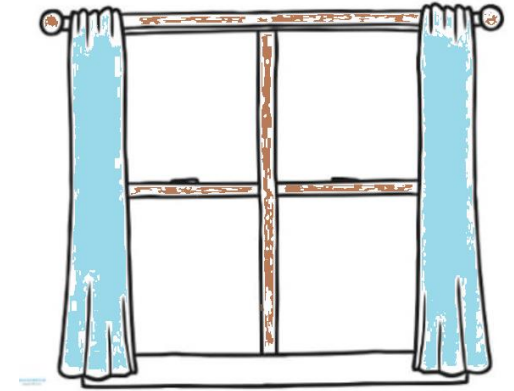
5 How much have you lost altogether? **4 counters**

# Bet 5

1 counter to play

Look out the window

If the next car that drives past is grey you win 3 counters



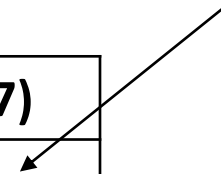
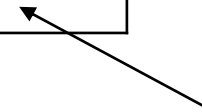
Take the bet

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 5        |              |           |

Not playing

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 5        | 0            |           |

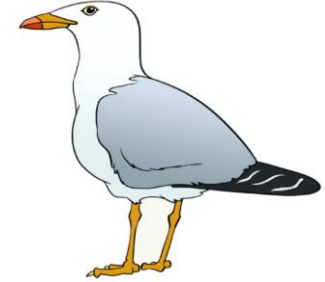
Update



1 counter to play

Look out the window for 5 seconds

If you see a seagull you win 4 counters



Take the bet

What's my chances?

Not playing

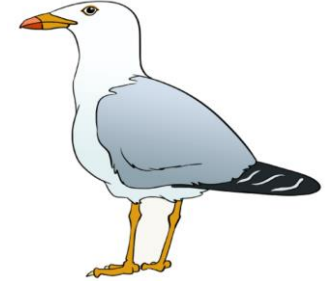
# What are my chances?

Back

1 counter to play

Look out the window for 5 seconds

If you see a seagull you win 4 counters



**Some probabilities are not obvious.**

There is no formula for this one. The only way you can work out if it is a good bet is to do an **experiment**.

For example you could look out the window for **5 minutes** and record how much of the time a seagull is in view.

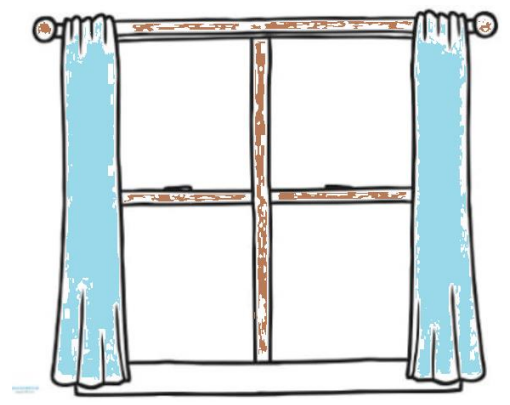
If you carry out these experiments you have to be aware of all the factors that may affect your answers. For example is there a time of day when there are more seagulls?



1 counter to play

Look out the window for 5 seconds

If you see a seagull you win 4 counters

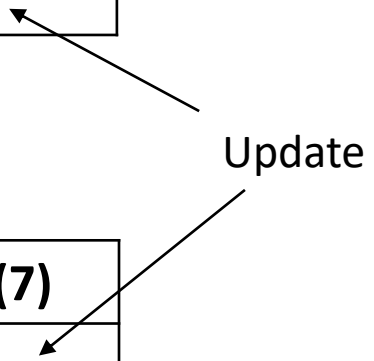


Take the bet

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 6        |              |           |

Not playing

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 6        | 0            |           |



# Bet 7

Back Next

1 counter to play

Pick a number from the board

If your number is chosen you win 8 counter



|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

- 1 What is the probability your number is chosen?
- 2 If you play the game 90 times how many would you expect to win?
- 3 How much will you expect to lose if you play the game 9 times?
- 4 How much will you expect to lose if you play 90 times?
- 5 What fraction of your counters do you lose when you play this game?

# Answers

Back Next

1 counter to play

Pick a number from the board

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

If your number is chosen you win 8 counter

1 What is the probability your number is chosen?

$$\frac{1}{9}$$

2 If you play the game 90 times how many would you expect to win?

$$\frac{1}{9} \times 90 = 10$$

3 How much will you expect to lose if you play the game 9 times?

1 counters

4 How much will you expect to lose if you play 90 times? 10 counters

5 What fraction of your money do you lose when you play this game?

$$\frac{1}{9}$$

1 counter to play


Pick a number from the board

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

If your number is chosen you win 8 counter

I ask year 7 students if they will take the bet.

There are **243 students** in year 7.  $\frac{2}{3}$  of the students take the bet.

- 1 How many students take the bet?
- 2 How many students should I expect to correctly guess the number?
- 3 How many counters in total will I give to those winners?
- 4 How many counters am I left with?
-  Can you create a formula to show how much I will make in counters?

Let  $p$  = probability of winning  
 $n$  = number of people betting

$c$  = cost to take bet  
 $w$  = how much they win

1 counter to play

Pick a number from the board

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

If your number is chosen you win 8 counter

There are **243 students** in year 7.  $\frac{2}{3}$  of the students take the bet.

1 How many students take the bet?

$$\frac{2}{3} \times 243 = 162$$

2 How many students should I expect to correctly guess the number?

$$\frac{1}{9} \times 162 = 18$$

3 How many counters in total will I give to those winners?

$$18 \times 8 = 144$$

4 How many counters am I left with?

$$162 - 144 = 18$$



*Click for explanation*

# Answers

Back Next

1 counter to play

Pick a number from the board

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

If your number is chosen you win 8 counter



Let  $p$  = probability of winning  
 $n$  = number of people betting

$c$  = cost to take bet  
 $w$  = how much they win

$$p = \frac{1}{9} \quad c = 1 \quad n = 162 \quad w = 8$$

Total counters in play  $162 \times 1 = 162$        $c \times n$

Number of winners  $162 \times \frac{1}{9} = 18$        $n \times p$

Total counters out  $18 \times 8 = 144$        $n \times p \times w$

Total counters left  $162 - 144 = 18$        $c \times n - n \times p \times w$       or      **Total =  $cn - npw$**

Test your formula

# Test your formula

Back Next

3 counter to play. Pick a number from the board

If your number is chosen you win 15 counters

500 people take the bet.

$$\text{Total} = cn - npw$$

|   |    |    |    |
|---|----|----|----|
| 1 | 2  | 3  | 4  |
| 5 | 6  | 7  | 8  |
| 9 | 10 | 11 | 12 |



# Answer

Back Next

3 counter to play. Pick a number from the board

If your number is chosen you win 15 counters

500 people take the bet.

|   |    |    |    |
|---|----|----|----|
| 1 | 2  | 3  | 4  |
| 5 | 6  | 7  | 8  |
| 9 | 10 | 11 | 12 |



$$\text{Total} = cn - npw$$

$$\text{Total} = 3 \times 500 - 500 \times \frac{1}{12} \times 15 = 875 \text{ counters}$$



# Bet 7

Back Next

1 counter to play

Pick a number from the board

If your number is chosen you win 8 counter

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

Take the bet

Not playing

# Update your table

Back Next

1 counter to play

Pick a number from the board

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | 9 |

If your number is chosen you win 8 counter

Take the bet

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 7        |              |           |

Not playing

| Question | +/- Counters | Total (7) |
|----------|--------------|-----------|
| 7        | 0            |           |

Update



# How did you do?

Back Next

**How many counters are you left with?**

**How much of a risk taker are you?**



# End of the lesson

Back

**Well done for completing the lesson.**



## Reflections

A large, empty rounded rectangular box with a black border, intended for students to write their reflections.